



## Operating envelope approach for grid-safe participation of distributed flexibility in balancing markets

**Wicak Ananduta**, L. Marques, A. Kaushal, A. Sanjab, T. Cuypers, and J. Vanschoenwinkel

# Outline

1 Distributed flexibility in balancing markets

2 Integrating operating envelopes

3 Analysis of the approach

4 Conclusion

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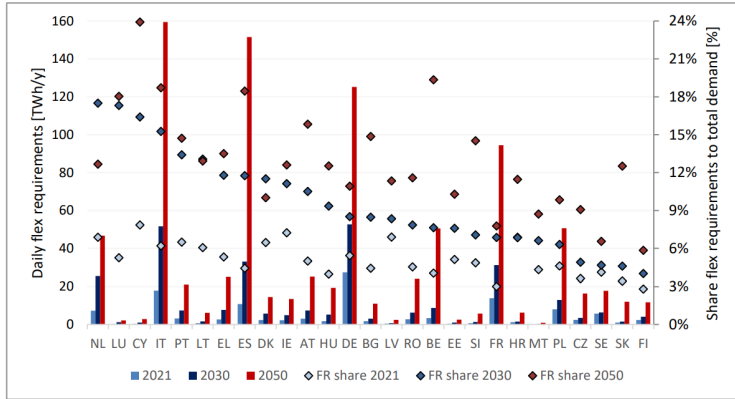
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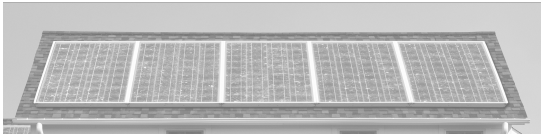
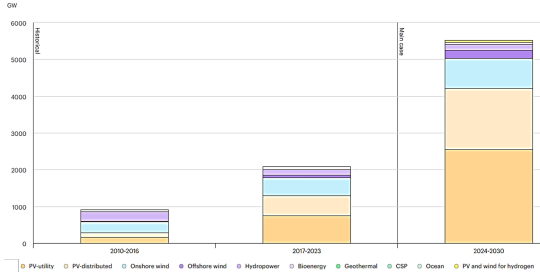
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# Flexibility requirements

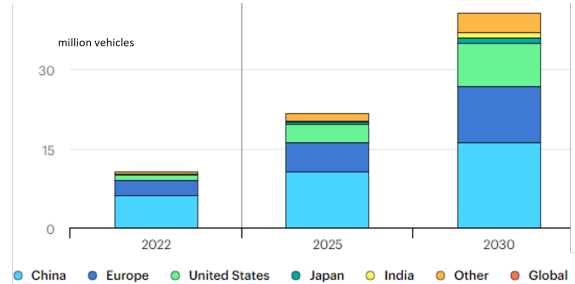


Daily flexibility requirements in Europe [Koolen, et, al., '23]

# Distributed flexibility



Renewable energy production [IEA '24]



EV sale projection [IEA '24]

# Balancing market

- Flexibility offers (upward/downward) in transmission (TN) and distribution (DN) networks:  
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- Responsibility, data confidentiality, communication intensive

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## Unsafe activation

Cleared offers located in DNs causing network problems

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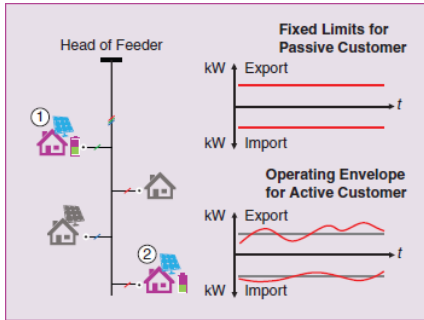
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# Operating envelopes (OEs)

## Definition

Allowable *dynamic* limits without causing network issues

- Depends on network current states

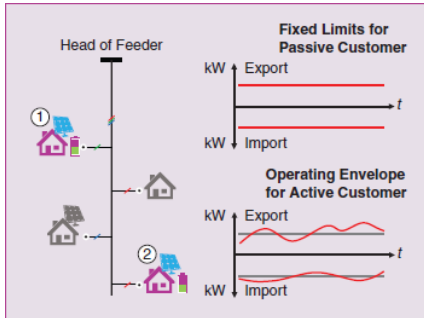


[Liu, et. al., PEM'21]

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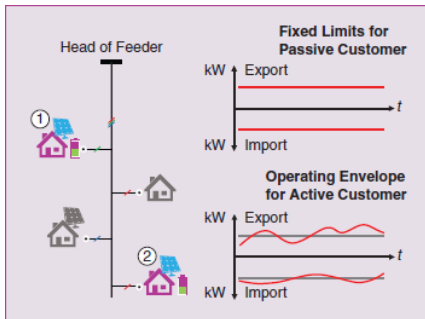
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$$OE_n : \{p_n | 0 \leq p_n \leq \varepsilon_n\}$$

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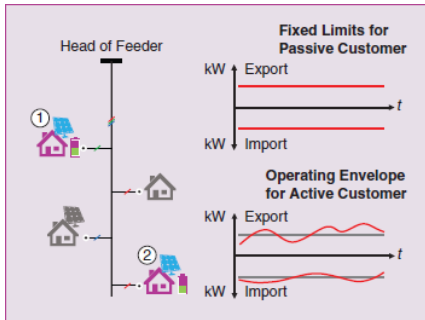
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- Calculation methods:
  - OPF-based: [Petrrou, et. al., TSG'21], [Liu, et. al., TSG'22], [Liu, et. al., 2023], [Feng, et. al., TSG'24],
  - Scenario/sampling based: [Riaz & Mancarella, '19], [Wang, et. al., AE'20], [Lankeshwara, et. al., TPS'24]

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## Research gaps

- How OEs impact balancing market outcomes
- Fundamental analysis

# OE-based balancing market

- Redefined market clearing problem:

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- No DNConst needed!

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- No DNConst needed!
- OEs as *simple* prequalification measure
- Network feasibility study in Belgium: static OE
- Compatible with existing regulation [Marques, et. al., Alexander D3.2, 2024]

# Optimization-based operating envelope calculation

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- Include DNConst → network model is crucial!
- Done for each DN

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## One-step method [Petrou, et. al., TSG'21]

- Compute  $OE_n$  for all resources
- Quadratic objective function:

$$\min \sum_{n \in \text{ResourcesDN}_m} w_n (\varepsilon_n - p_n^{\max})^2$$

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## Two-step method [Liu, et. al., TSG'22]

- Compute  $OE_n$  for downward and upward resources separately
- Linear objective function:

$$\max \sum_{n \in \text{ResourcesDN}_m} w_n \cdot \varepsilon_n$$

# Optimization-based operating envelope calculation (+)

- Different weight  $w_n$  types:

- Equal,

$$w_n = 1, \quad \text{for all resources}$$

- Price-based:

$$w_n \propto \begin{cases} |\text{price}_n|, & \text{for all downward resources} \\ 1/|\text{price}_n|, & \text{for all upward resources} \end{cases}$$

- Quantity-based:

$$w_n = p_n^{\max}, \quad \text{for all resources}$$

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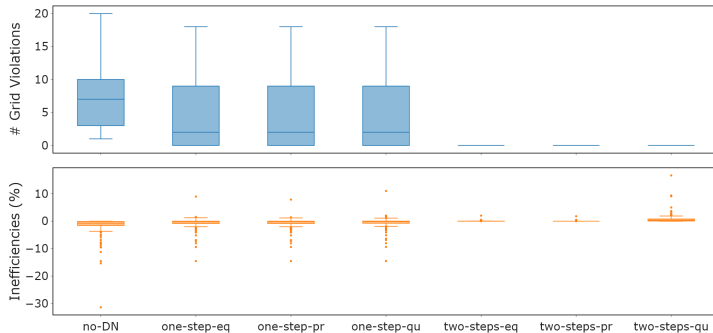
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Assessing performance of integrating OEs into balancing market:

- Grid safety of cleared offers
  - Satisfaction of voltage and line flow limits (DNConst)
  - DNConst uses linearized branch flow model
- Market efficiency
  - Total flexibility procurement cost
  - Benchmarked with idealized formulation
- Volume of unqualified DN offers

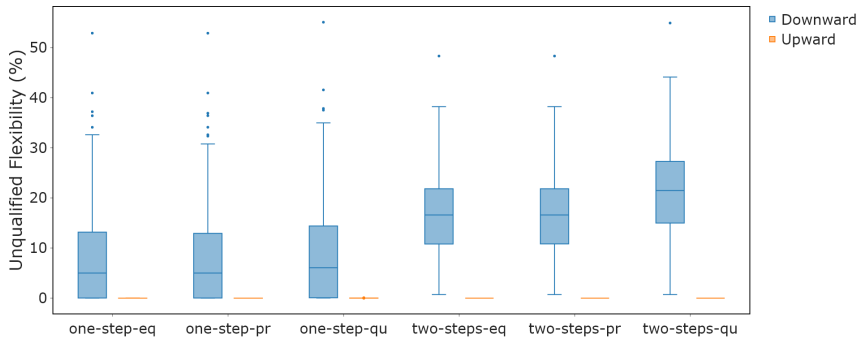
# Numerical tests (+) [Kaushal, et. al., ISGT'24]

- ~ 300 cases (downward scenario) where (BM *no-DN*) is not grid safe
  - IEEE 14-bus TN coupled with Matpower 69-bus and 141-bus DNs
  - Monte Carlo simulations: randomly generated loads, generation, flexibility offers



- 2-step OE **always** provides grid-safe (but possibly suboptimal) outcomes
- 1-step OE does not always provide grid-safe outcomes
- Price-based weight is best in market efficiency

# Numerical tests (++) [Kaushal, et. al., ISGT'24]



- 2-step OE provides more restricted limits than 1-step OE

# Theoretical results

- DNConst is linearized branch flow model [Sanjab, et. al., '21]
- Distribution networks are radial
- Prices of upward resources are more expensive than downward resources

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## (Theorem) Grid safety guarantee

If  $OE_n$  calculated with **2-step method**, outcomes of (BM-OE),  $(p_n^*)_{n \in \text{Resources}}$  are grid safe, i.e.,

$$\exists \varphi^{\text{DN}_m} \mid (p_n^*)_{n \in \text{ResourcesDN}_m} \in \text{DNConst}(\varphi^{\text{DN}_m}), \quad \forall m \in \text{DNs}.$$

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## (Proposition) Suboptimality

Outcomes are suboptimal and inefficiency of (BM-OE) can be upper-bounded by

$$\sum_{m \in \text{DNs}} \sum_{n \in \text{ResourcesDN}_m} \text{price}_n(p_n^* - \hat{p}_n),$$

where  $(\hat{p}_n)_{n \in \text{Resources}}$  are outcomes of (BM).

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## Publications:

- “Development of a novel, grid safe concept for flexibility provision from the LV grid,” Alexander D3.2.
- “Embedding operating envelopes in the market design to unlock the flexibility potential of distribution grids,” CIRED Vienna Workshop, 2024.
- “Operating envelopes for the grid-constrained use of distributed flexibility in balancing markets,” ISGT Europe Conference, 2024.  
*Best paper award!*
- “Grid-safe flexibility market design based on the operating envelope approach,” in preparation for journal submission.



This project has received funding from Energy Transition Fund 2021 FPS Economy, SMEs, Self-employed and Energy.

<https://alexander-project.vito.be/en>

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